SOME REMARKS ON COMPLETELY α-IRRESOLUTE FUNCTIONS

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#### **Abstract**

Chae *et al.* [4] (resp. Navalagi G. B. [14]) have studied the concept of NA-continuous (resp. completely  $\alpha$ -irresolute) functions. Now, the aim of this paper we note that NA-continuous functions and completely  $\alpha$ -irresolute functions are the same definitions. Also, we investigate several new properties of completely  $\alpha$ -irresolute functions are obtained. It is shown that, if  $f_1$  and  $f_2$  are completely  $\alpha$ -irresolute functions of a space X into an  $\alpha$ -Hausdorff space Y, then the set  $\{x \in X: f_1(x) = f_2(x)\}$  is  $\delta$ -closed in X.

### 1. INTRODUCTION

Njastad O. [15] defined an  $\alpha$ -set in a space as a set S such that  $S \subset Int(Cl(Int(S)))$ . Maheshwari S. N. [11] defined a feebly open set as a set S such that there exists an open set U such that  $U \subset S \subset sCl(U)$ , where sCl(U) denotes the semi-closure operator. It was shown in [7] that  $\alpha$ -sets and feebly open sets are the same sets in any space. Recently, Chae *et al.* [4] (resp. Navalagi G. B.[14]) have studied the concept of NAcontinuous (resp. completely  $\alpha$ -irresolute) functions. Now, in the present paper we note that NA-continuous functions and completely  $\alpha$ -irresolute functions are the same definitions. It is known in Chae *et al.* (1986) that the type of NA-continuous functions is stronger than the class of super-continuous functions due to Munshi [13], and weaker than the class of strongly continuous functions due to Arya S. P.[1].

The purpose of the present paper is to investigate further properties of completely  $\alpha$ -irresolute functions.

#### 2. PRELIMINARIES

Throughout the present paper, spaces always mean topological spaces on which no separation axiom is assumed unless explicitly stated. Let S be a subset of a

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space X. The closure of S and the interior of S are denoted by Cl(S) and Int(S), respectively. A subset S is said to be  $\alpha$ -open [15] (resp.  $\theta$ -open [19]) if S  $\subset$  Int(Cl(Int(S)))(resp. if for each  $x \in S$ , there exists an open set U in X such that  $x \in U \subset Cl(U) \subset S$  [17]). It is well-known that for a space  $(X, \tau)$ , X can be retopologized by the family  $\tau^{\alpha}$  of all  $\alpha$ -open sets of X[10] and also the family  $\tau^{\theta}$  of all  $\theta$ -open set of X[19], that is,  $\tau^{\theta}$  (called  $\theta$ -topology) and  $\tau^{\alpha}$  (called an  $\alpha$ -topology) are topologies on X, and it is obvious that  $\tau^{\theta} \subset \tau \subset \tau^{\alpha}$ .

A subset S of a space X is called regular open (resp. regular closed ) set if S = Int (Cl(S)) (resp. S= Cl(Int(S)). A subset S of a space X is called  $\delta$ -open [19] for each  $x \in S$ , there exists an open set U in X such that  $x \in U \subset Int(Cl(U)) \subset S$ . The family of all  $\alpha$ -open (resp. regular open,  $\theta$ -open and  $\delta$ -open) sets of X is denoted by  $\alpha O(X)$ (resp. RO(X),  $\theta O(X)$  and  $\delta O(X)$ ). The complement of an  $\alpha$ -open (resp. regular open,  $\theta$ -open and  $\delta$ -open) sets of X is called  $\alpha$ -closed (resp. regular closed,  $\theta$ -closed and  $\delta$ -closed) set.

A function  $f: X \rightarrow Y$  is said to be  $\alpha$ -strongly  $\theta$ -continuous [5] if for each  $x \in X$  and each  $\alpha$ -open set H of Y containing f(x), there exists an open set U of X containing x such that  $f(Cl(U)) \subset H$ . A function  $f: X \rightarrow Y$  is said to be strongly  $\alpha$ -irresolute[6] (resp. NA-continuous [4]) if and only if for each  $\alpha$ -open (resp. feebly open) subset H of Y,  $f^{-1}(H)$  is open (resp.  $\delta$ -open) in X. A space X is said to be an extremely disconnected [18, p.32] if the closure of each open set of X is open in X. A space X is said to be semi-regular if the family of regularly open sets forms a base for the topology of X. A subset S of a space X is said to be S-closed [16] relative to S if each cover S if S by open sets of S, there exists a finite subset S of S such that  $S \subset U$  and S if S by open sets of S in S i

#### 3. MAIN RESULTS

DEFINITION 3.1[14]: A function  $f: X \rightarrow Y$  is said to be completely  $\alpha$ -irresolute if the inverse image of each  $\alpha$ -open set of Y is regular open in X.

THEOREM 3.1: Let  $f: X \to Y$  be a function. Let  $\mathcal{B}$  be any basis for  $\sigma^{\alpha}$  in Y. Then f is completely  $\alpha$ -irresolute functions if and only if for each  $B \in \mathcal{B}$ ,  $f^{-1}(B)$  is a regular open subset of X.

LEMMA 3.1[20]: Let  $R \in RO(A)$  and  $A \in RO(X)$ , then  $R \in RO(X)$ .

THEOREM 3.2: Let  $f: X \rightarrow Y$  be any function. If for each  $x \in X$ , there exists a regular open set R containing x such that  $f \mid R$  is completely  $\alpha$ -irresolute function, then f is completely  $\alpha$ -irresolute function.

**PROOF:** Let  $x \in X$  and let H be any  $\alpha$ -open subset containing f(x). Then, there exists a regular open set R containing x such that  $f \mid R$  is completely  $\alpha$ -irresolute function. Therefore, by [14, Theorem 3.3], there exists a regular open set W in R containing x such that  $f|_{R}(W) \subset H$ . Since R is regular open. Therefore, by Lemma 3.1, W is regular open in X and hence  $f(W) \subset H$ . Thus, f is completely  $\alpha$ -irresolute function.

**LEMMA 3.2:** If  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute function, then  $f^{-1}(V)$  is regular closed for any nowhere dense subset V of Y.

**PROOF:** Let V be any nowhere dense in Y. Then  $Int(Cl(V)) = X \setminus Int(X \setminus V)$ . Thus, we have  $X = Int(Cl(Int((X \setminus V)))$ , for  $Int(Cl(V)) = \emptyset$ . Thus,  $Y \setminus V$  is  $\alpha$ -open in Y. Hence  $f^{-1}(V)$  is regular closed in X since  $f^{-1}(Y \setminus V) = X \setminus f^{-1}(V)$  is regular open and f is completely  $\alpha$ -irresolute function.

# **THEOREM 3.3:** (Restricting the range)

If  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute function and f(X) is taken with the subspace topology, then  $f: X \rightarrow f(X)$  is completely  $\alpha$ -irresolute function.

**PROOF:**  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute function implies  $f^{-1}(H)$  is regular open, where H is some  $\alpha$ -open subset of Y. Now  $f^{-1}[H \cap f(X)] = f^{-1}(H) \cap f^{-1}[f(X)] = f^{-1}(H) \cap X = f^{-1}(H)$  is regular open. Therefore,  $f: X \rightarrow f(X)$  is completely  $\alpha$ -irresolute function.

**THEOREM 3.4:** Let X be an extremely disconnected. If  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute function, then it is  $\alpha$ -strongly  $\theta$ -continuous function.

**PROOF:** Suppose that X is an extremely disconnected and f is completely  $\alpha$ -irresolute function. Let H be any  $\alpha$ -open set of Y. Since f is completely  $\alpha$ -irresolute function. Therefore,  $f^{-1}(H)$  is regular open in X. But X is an extremely disconnected. Then, by [3, Lemma 2.18],  $f^{-1}(H)$  is  $\theta$ -open. Thus, by [5, Theorem 2], f is  $\alpha$ -strongly  $\theta$ -continuous.

**DEFINITION 3.2:** A space X is said to be r-disconnected if there exists two regular open sets R and W such that  $X = R \cup W$  and  $R \cap W = \phi$ , otherwise X is called r-connected.

**THEOREM 3.5:** If X is r-connected space and  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute surjection, then Y is  $\alpha$ -connected.

**PROOF:** Suppose Y is not  $\alpha$ -connected. Then, there exist non empty  $\alpha$ -open sets  $H_1$  and  $H_2$  in Y such that  $H_1 \cap H_2 = \emptyset$  and  $H_1 \cup H_2 = Y$  and since f is completely

 $\alpha$ -irresolute functions, then we have  $f^{-1}(H_1) \cap f^{-1}(H_2) = \phi$  and  $f^{-1}(H_1) \cup f^{-1}(H_2) = X$ . Since f is surjection, then  $f^{-1}(H_j) \neq \phi$  and  $f^{-1}(H_j) \in RO(X)$ , for j = 1, 2. This indicated that X is not r-connected. This is a contradiction.

**COROLLARY 3.1:** Let A be r-connected subset of a topological space X, and let f be a completely a-irresolute function of X into a topological space Y. Then f(A) is  $\alpha$ -connected.

**THEOREM 3.6:** For a topological space X to be r-disconnected it is necessary and sufficient that there exists a surjection completely  $\alpha$ -irresolute function of X onto a discrete space containing more than one point.

**PROOF:** The condition is sufficient by Theorem 3.5.

Conversely, if X is r-disconnected, there exist two non empty disjoint regular open subsets R and W whose union is X, and the function f of X onto a discrete space of two elements  $\{a, b\}$ , defined by  $f(A) = \{a\}$  and  $f(B) = \{b\}$ , is completely  $\alpha$ -irresolute function.

**THEOREM 3.7:** Let  $f: X \rightarrow Y$  be a strongly  $\alpha$ -irresolute function from a semiregular space X into Y. Then f is completely  $\alpha$ -irresolute

**PROOF:** Let  $x \in X$  and H be an  $\alpha$ -open set containing f(x). Then ,  $f^{-1}(H)$  is open in X since f is strongly  $\alpha$ -irresolute. Therefore, there is an open subset U of x such that  $x \in U \in Int(Cl(U)) \subset f^{-1}(H)$ , since X is semi-regular. Hence f is completely  $\alpha$ -irresolute function.

**REMARK 3.1:** Every open set in a T<sub>3</sub>-space can be written as the union of regular open sets.

**COROLLARY 3.2:** Let X be a  $T_3$ -topological space and let  $f: X \rightarrow Y$  be strongly  $\alpha$ -irresolute, then f is completely  $\alpha$ -irresolute function.

**PROOF:** Every regular (or  $T_3$ ) space is semi-regular.

**DEFINITION 3.3:** A space X is said to be  $\alpha$ -Hausdorff [6](resp. rT<sub>2</sub> [2]) if for any x, y  $\in$  X, x $\neq$ y, there exist  $\alpha$ -open(resp. regular open) sets G and H such that x  $\in$  G, y  $\in$  H and G  $\cap$  H =  $\phi$ .

**THEOREM 3.8:** Let  $f: X \rightarrow Y$  be injective and completely  $\alpha$ -irresolute function. If Y is  $\alpha$ -Hausdorff space, then X is  $rT_2$ .

**PROOF:** Let x and y be any two distinct points of X . Since f is injective,  $f(x) \neq f(y)$ . Now, Y being an  $\alpha$ -Hausdorff space, there exist two disjoint  $\alpha$ -open sets G

and H such that  $f(x) \in G$ ,  $f(y) \in H$ . Since f is completely  $\alpha$ -irresolute function, it follows that  $f^{-1}(G)$  and  $f^{-1}(H)$  are disjoint regular open sets containing x and y, respectively. Hence X is  $rT_2$ .

Recall that a space  $(X, \tau)$ , X is called  $\alpha$ -compact [8] if every  $\alpha$ -open cover of X has a finite subcover.

**DEFINITION 3.4:** For a space  $(X, \tau)$ , let A be a subset of X. Then A is said to be  $\alpha$ -compact relative to X [8] if every cover of A by  $\alpha$ -open sets of X has a finite subcover.

**THEOREM 3.9:** If  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute function and F is N-closed subspace relative to X, then f(F) is  $\alpha$ -compact relative to Y.

**PROOF:** Let  $\{H_i : i \in I\}$  be a cover of f(F) by  $\alpha$ -open sets in Y. For each  $x \in F$ , there exists an  $i(x) \in I$  such that  $f(x) \in H_{i(x)}$ . Since f is completely  $\alpha$ -irresolute function, there exists a regular open set  $R_x$  of x such that  $f(R_x) \subset H_{i(x)}$ . The family  $\{R_x : x \in F\}$  is a regular open cover of F. For some finite subset  $F_0$  of F, we have  $F \subset \{R_x : x \in F_0\}$  and hence  $f(F) \subset \{H_{i(x)} : x \in F_0\}$ . This shows that f(F) is  $\alpha$ -compact relative to Y.

**THEOREM 3.10:** Let  $g: X \to Y_1 \times Y_2$  be completely  $\alpha$ -irresolute function, where  $X, Y_1$  and  $Y_2$  are any topological spaces. Let  $f_i: X \to Y_i$  defined as follows:

For  $x \in X$ ,  $g(x) = (x_1, x_2)$ ,  $f_i(x) = x_i$  for i = 1, 2. Then  $f_i : X \rightarrow Y_i$  is completely  $\alpha$ -irresolute function, for i = 1, 2.

**PROOF:** Let x be any point in X and  $H_1$  be any  $\alpha$ -open set of  $Y_1$  containing  $f_1(x) = x_1$ , then  $H_1 \times Y_2$  is  $\alpha$ -open in  $Y_1 \times Y_2$ , which contain  $(x_1, x_2)$ .

Since g is completely  $\alpha$ -irresolute function. Therefore, by [14, Theorem 3.3], there exists a regular open set R containing x such that  $g(R) \subset H_1 \times Y_2$ . Then  $f_1(R) \times f_2(R) \subset H_1 \times Y_2$ . Therefore,  $f_1(R) \subset H_1$ . Hence  $f_1$  is completely  $\alpha$ -irresolute function. Similar statement for  $f_2$  is completely  $\alpha$ -irresolute function.

**THEOREM 3.11:** If  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute function,  $g: X \rightarrow Y$  is continuous and Y is Hausdorff, then the set  $\{y \in X : f(y) = g(y)\}$  is  $\delta$ -closed in X.

**PROOF:** Let  $A = \{y \in X : f(y) = g(y)\}$  and  $x \in X \setminus A$ . Then  $f(x) \neq g(x)$ . Since Y is Hausdorff, there exist open ( $\alpha$ -open) sets  $H_1$  and  $H_2$  in Y such that  $f(x) \in H_1$ ,  $g(x) \in H_2$  and  $H_1 \cap H_2 = \emptyset$ . Since f is completely  $\alpha$ -irresolute function. Therefore, by [4, Theorem 2.1], there exists a regular open set R containing x such that  $f(R) \subset H_1$ . Since g is continuous, there exists an open set U in X containing x such that g

(U)  $\subset$  H<sub>2</sub>. Now, put R\* = R  $\cap$  U, then by [4, Lemma 2.6], R\* is regular open set in the subspace R and hence it is regular open in X containing x and  $f(R^*) \cap g(R^*)$   $\subset$  H<sub>1</sub>  $\cap$  H<sub>2</sub> =  $\phi$ . Therefore, we obtain R\*  $\cap$  A =  $\phi$ . This shows that A is  $\delta$ -closed in X.

**THEOREM 3.11:** If  $f_1$  and  $f_2$  are completely  $\alpha$ -irresolute functions of a space X into an  $\alpha$ -Hausdorff space Y, then the set  $\{x \in X: f_1(x) = f_2(x)\}$  is  $\delta$ -closed in X.

**PROOF:** Let  $A = \{x \in X : f_1(x) = f_2(x)\}$ . If  $x \in X \setminus A$ , then we have  $f_1(x) \neq f_2(x)$ . Since Y is  $\alpha$ -Hausdorff, there exist  $\alpha$ -open sets  $H_1$  and  $H_2$  in Y such that  $f_1(x) \in H_1$ ,  $f_2(x) \in H_2$  and  $H_1 \cap H_2 = \phi$ . Since  $f_j$  is completely  $\alpha$ -irresolute functions, there exists a regular open set  $R_j$  in X containing x such that  $f_j(R_j) \subset H_j$ , where j = 1, 2. Put  $R = R_1 \cap R_2$ , then R is a regular open set in X containing x and  $f_1(R) \cap f_2(R) \subset R_1 \cap R_2 = \phi$ . This implies that  $R \cap A = \phi$  and hence A is  $\delta$ -closed in X.

**LEMMA 3.2[12]:** Let  $X_1$  and  $X_2$  be topological spaces with topologies  $\tau_1$  and  $\tau_2$ , respectively. Let  $\tau_{\delta 1}$  and  $\tau_{\delta 2}$  denote the topologies generated by regularly open sets of  $X_1$  and  $X_2$ , respectively. If  $\tau$  denote the product topology of  $X_1 \times X_2$  and  $\tau_{\delta}$  denote the topology generated by the regularly open sets of  $X_1 \times X_2$ , then  $\tau_{\delta 1} \times \tau_{\delta 2} = \tau_{\delta}$ .

**THEOREM 3.13:** If Y is an  $\alpha$ -Hausdorff space and  $f: X \rightarrow Y$  is completely  $\alpha$ -irresolute function, then the set  $A = \{(x_1, x_2): f(x_1) = f(x_2)\}$  is  $\delta$ -closed in the product space  $X \times X$ .

**PROOF:** If  $(x_1, x_2) \in X \times (X \setminus A)$ , then we have  $f(x_1) \neq f(x_2)$ . Since Y is  $\alpha$ -Hausdorff, there exist  $\alpha$ -open sets  $H_1$  and  $H_2$  in Y such that  $f(x_1) \in H_1$ ,  $f(x_2) \in H_2$  and  $H_1 \cap H_2 = \emptyset$ . Since f is completely  $\alpha$ -irresolute function. Therefore, by [4, Theorem 2.1], there exists a  $\delta$ -open set  $U_j$  containing  $x_j$  such that  $f(U_j) \subset H_j$ , where j = 1, 2.

Put  $U = U_1 \times U_2$ , then by Lemma 3.2, that U is a  $\delta$ -open set in X×X containing  $(x_1, x_2)$  and  $A \cap U = \phi$ . This shows that A is  $\delta$ -closed in the product space X×X.

**THEOREM 3.14:** If  $f_i: X_i \to Y_i$  is completely  $\alpha$ -irresolute function, for i = 1, 2. Let  $f: X_1 \times X_2 \to Y_1 \times Y_2$  be a function defined as follows:

 $f(\mathbf{x}_1, \mathbf{x}_2) = (f_1(\mathbf{x}_1), f_2(\mathbf{x}_2))$ . Then f is completely  $\alpha$ -irresolute function.

**PROOF:** Let  $H_1 \times H_2 \subset Y_1 \times Y_2$ , where  $H_i$  is α-open in  $Y_i$ , for i = 1, 2, then  $f^{-1}(H_1 \times H_2) = f_1^{-1}(H_1) \times f_2^{-1}(H_2)$ , since  $f_i$  is completely α-irresolute function, for i = 1, 2. By, Definition 3.1 and Theorem 3.10 of [9],  $f^{-1}(H_1 \times H_2)$  is regular open in  $X_1 \times X_2$ . Now if H is any α-open subset of  $Y_1 \times Y_2$ , then  $f^{-1}(H) = f^{-1}(\bigcup H_\alpha)$ , where  $H_\alpha$  is of the form  $H_{\alpha 1} \times H_{\alpha 2}$ . Therefore, by Lemma 3.2,  $f^{-1}(H) = \bigcup f^{-1}(H_\alpha)$  is δ-open in  $X_1 \times X_2$ , which completes the proof.

**THEOREM 3.15:** Let  $f: X \rightarrow Y$  be a completely  $\alpha$ -irresolute function on X into an  $\alpha$ -Hausdorff space Y. If M is an  $\alpha$ -compact subset of Y, then  $f^{-1}(M)$  is a  $\delta$ -closed subset of X.

**PROOF:** Suppose  $f^{-1}(M)$  is not  $\delta$ -closed in X. Then, there exists an  $x \in IntCl(f^{-1}(M))$ , but  $x \notin f^{-1}(M)$ , it follows that  $f(x) \neq m$ . Now for each  $m \in M$ , there exist  $\alpha$ -open sets  $W_m(f(x))$  and H(m) containing f(x) and m, respectively such that

 $W_m(f(x)) \cap H(m) = \phi$  because Y is  $\alpha$ -Hausdorff. By construction,  $M \subset \bigcup_{m \in M} H(m)$ , and since M is  $\alpha$ -compact. Therefore, there exists a finite subfamily  $\{H(m) : i = 1, \}$ 

2,..., n} such that 
$$M \subset \bigcup_{i=1}^n H(m_i)$$
. Let  $H^* = \bigcup_{i=1}^n H(m_i)$  and  $W^* = \bigcap_{i=1}^n W_{m_i}(f(x))$ .

Then  $M \subset H^*$  and  $H^* \cap W^* = \emptyset$ . Since each  $W_{m_i}(f(x))$  is an  $\alpha$ -open set of f(x), it follows that  $W^*$  is an  $\alpha$ -open set of f(x). Since f is completely  $\alpha$ -irresolute function. Therefore, by [4, Theorem 3.3], there exists a regular open set U containing x such that  $f(U) \subset W^*$ . But  $x \in IntCl(f^{-1}(M))$ . Therefore,  $U \cap f^{-1}(M) \neq \emptyset$ . Hence there exists  $z \in U \cap f^{-1}(M)$ , and so  $f(z) \in f(U) \cap M \subset W^* \cap M \subset W^* \cap H^* = \emptyset$ , which is contradiction. Hence  $f^{-1}(M)$  is  $\delta$ -closed.

Since every compactness implies  $\alpha$ -compactness, we obtain from Theorem 3.15 the following corollary.

**COROLLARY 3.3:** For completely  $\alpha$ -irresolute functions into  $\alpha$ -Hausdorff spaces, the inverse image of each compact set is  $\delta$ -closed.

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