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### Sixth Order Model of Wind Turbine Voltage Flicker Taking Into Account Impact of Vertical Wind Shear

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**Abstract :** Various flicker models are developed by researchers. Each model has its own drawback. In this model various order models are compared. The models consist of various wind turbine parameters like number of wind turbine blades, wind turbine blade length and wind turbine blade width. Sixth order model is most suitable for wind turbine voltage flicker.

**Keywords :** Voltage Flicker; vertical wind shear; wind turbine; wind energy.

#### 1. CURVE FITTING

In curve fitting a curve can be constructed. That curve is best fitted to a series of data points. In curve fitting mathematical function can also be formed. In curve fitting interpolation is used. In interpolation exact fit to data is required. In curve fitting smoothing also be used. In smoothing smooth function is used. In smooth function data is fitted approximately. Sometimes regression analysis is also used. In regression analysis uncertainty of fitting the curve with data is found. Fitted curve is useful in finding the missing data. With fitted curve relation between two variables can be found. In extrapolation fitted curve is used to find the data beyond range of observed data.

Mark E Weber studied the radars used for ground based wind shear. Wind shear with low altitude consisting of thunder storm outflow hampers the operation of the airplane severely while take off and landing. Doppler weather radars are installed at airport to provide wind data to the pilot. These Doppler radars detect wind shear and protects airplane. He provided comparative analysis of radar with various points like radar sensitivity, ground clutter, rejection capability etc. [13]

Xue Zhu LV studied impact of vertical wind shear on hurricane eye. Powerful winds are generated by tropical cyclones. Torrential rainfall is also caused by tropical cyclones. Prediction of cyclone is also significant task for meteorologists. Hurricane eyes are normally circular on satellite images. [15]

Q Jin computed availability of wind farm taking into account impact of vertical wind shear. He studied wind speed distribution. He computed the wind speed at 60 m using power law. He used least square method, modified methods to compute wind parameters. Wind speed changes with height because of friction of surface. [18]

K Reddondo studied the measurement of flicker in wind turbines. He used digital differentiation for voltage flicker measurement. He used high rate of sampling. The he performed analysis using simulated waveforms and field measurement in Spain. The frequency response of digital differentiation is important in computing voltage flicker. [21]

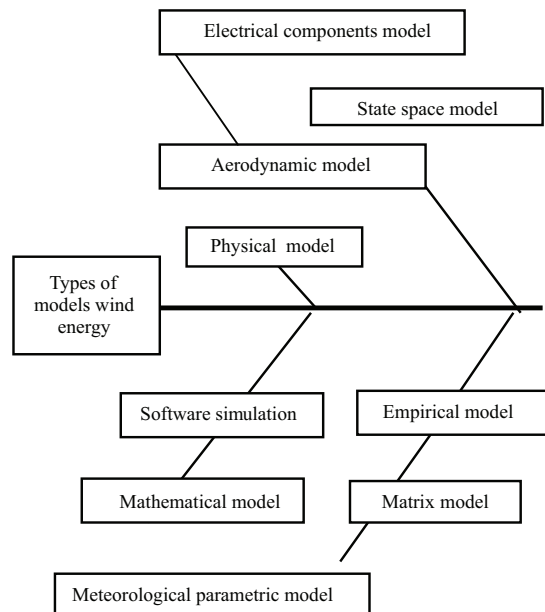
J.J. Gutierrez studied voltage flicker measurement for wind generation system. He developed a system to assess voltage flicker. His research is useful in certification of wind turbines. In his voltage flicker measurement system there are two modules. The first module is a signal register in which established voltage and current series according to wind speed is stored. The second module processes the stored series in comparison with standard data. The equipment developed by him can store data of three phases [1]

H Kasem developed a voltage flicker minimization technique in doubly fed induction generator wind energy system using reactive current management. Due to voltage variation in wind turbines there is a limitation in connection of wind power to the grid. Ali H Kasem developed a voltage flicker reduction algorithm. In the algorithm optimal reactive current flow is used. The modeling of wind turbine system is done in Matlab. Kasem considered the losses occurred due to reactive power flow in his flicker mitigation system. He developed a mathematical equation for reactive current of rotor. It is used to reduce the losses of doubly fed induction generator under various conditions of power factor. [24]

## 2. FITTING OTHER CURVES TO DATA POINTS

A range of curves is used. The curve may be elliptical, hyperbolic and circular. Sometimes trigonometric functions are utilized as well. In trigonometric function sine and cosine function may be used. For trajectories of objects, parabolic curve can be used. For tidal data, sine wave may also be used. Sometimes addition of two sine waves may be utilized to consider sun and moon effect.

## 3. VARIOUS MODELS FOR WIND ENERGY



**Figure 1: Various of models of wind energy**

Various types of models can be developed for wind generation system. Fig. 1 gives various types of models that can be developed for wind energy. In this paper empirical model of voltage flicker initiated in a wind turbine is developed.

Fig. 1 gives various models of wind energy. Physical model most commonly referred to simply as a model is a smaller or larger physical copy of an object. The object being modeled may be small (for example, an atom) or large (for example, the Solar System).

Aerodynamic model of wind turbine can be developed. Aerodynamics is a branch of dynamics concerned with studying the motion of air, particularly when it interacts with a solid object, such as an airplane wing. Aerodynamics is a sub-field of fluid dynamics and gas dynamics, and many aspects of aerodynamics theory are common to these fields. The term aerodynamics is often used synonymously with gas dynamics, with the difference being that “gas dynamics” applies to the study of the motion of all gases, not limited to air.

In models using electrical components, model of generators, transformers and transmission lines can be developed using elements like resistors, inductors and capacitors. In wind energy system model of wind generator can be developed. Models of squirrel cage induction generator, slip ring induction generator and permanent magnet synchronous generator can be developed.

Software simulation models can be developed in various software like Matlab, PSCAD and Etap etc. Complete wind energy system can be simulated in a software. By changing various parameters system can be studied.

Meteorological model are developed using meteorological parameters like wind speed turbulence intensity etc. In this research impact of vertical wind shear on voltage flicker initiated in wind turbine is studied.

Empirical modeling refers to any kind of modeling based on empirical observations rather than on mathematically describable relationships of the system modeled. In this research , empirical model of voltage flicker is developed.

A mathematical model is a description of a system using mathematical concepts. The process of developing a mathematical model is termed mathematical modeling. Mathematical models are used not only in the natural sciences such as physics, biology, earth science, meteorology and engineering disciplines like computer science, artificial intelligence, but also in the social sciences like economics, psychology, sociology and political science. Physicists, engineers, statisticians, operations research analysts and economists use mathematical models most extensively. A model may help to explain a system and to study the effects of different components, and to make predictions about behavior

In control engineering, a state-space representation is a mathematical model of a physical system as a set of input, output and state variables related by first-order differential equations. “State space” refers to the space whose axes are the state variables. The state of the system can be represented as a vector within that space.

Sometimes matrix models are also developed. In mathematics, a matrix is a rectangular array of numbers, symbols, or expressions, arranged in rows and columns. The individual items in a matrix are called its elements or entries

#### **4. ASSUMPTIONS MADE WHILE PROPOSING VOLTAGE FLICKER MODELS**

This section gives various assumptions made during development of the models of voltage flicker initiated in a wind turbine due to vertical wind shear

1. The tower considered is a tubular tower as for larger turbines lattice tower is not favored. Even for lattice tower 3  $p$  effect will be dissimilar than tubular

2. Wind turbine considered is of large size ranging from 1 MW to 7 MW.
3. Wind speed ricocheted is in between cut in and cut out speed. Normally cut in speed is 3 m/s, cut out speed is 25 m/s and rated speed is 11 m/s. Wind turbines operate in this speed range and are connected to grid.
4. Turbine is upwind turbine. Majority of the turbines are upwind turbines and downwind turbines are rarely used.

## 5. PROPOSED SIXTH ORDER MODEL OF VOLTAGE FLICKER IN WIND TURBINE

Equation 1 is a proposed six order equation.

$$P_s = V_{shr}^6 - B V_{shr}^5 + C V_{shr}^4 - D V_{shr}^3 + E V_{shr}^2 - F V_{shr} + G \quad (1)$$

Table 1 gives look up table for proposed sixth order model. The values in the look up table are found from the experiment on the wind turbine in a laboratory test set up.

**Table 1**  
Look up table for proposed sixth order model

Constant	Value
A	0.054
B	1.703
C	21.835
D	146.18
E	538.61
F	1034
G	809.02

Fig. 2 gives comparison of curve fitting model of voltage flicker and proposed sixth order model. The model is represented by a dotted line. Sixth order model is represented by a continuous line.

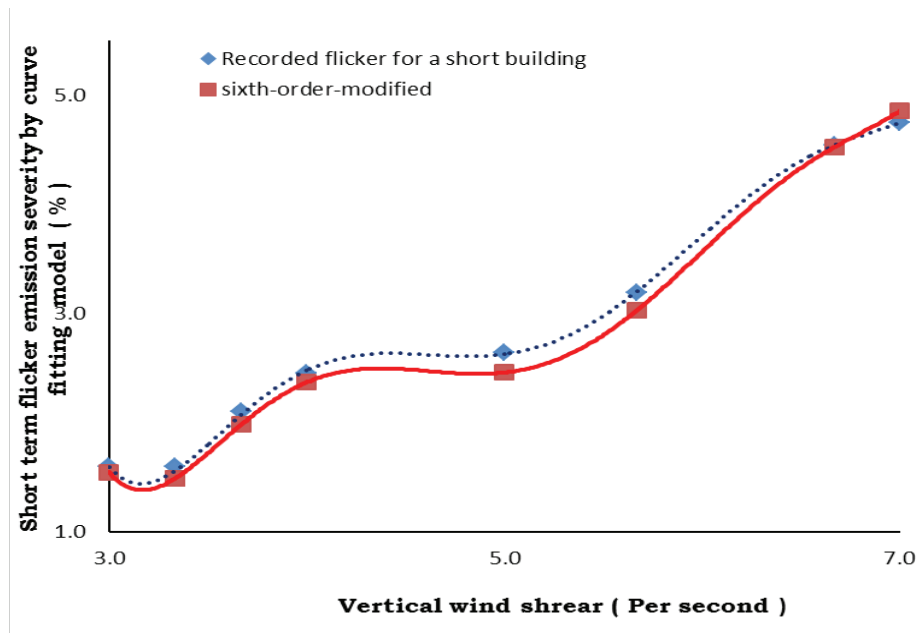


Figure 2: Sixth order model or hexic model or sextic model

## 6. PROPOSED SIXTH ORDER MODELS FOR DIFFERENT NUMBER OF BLADES

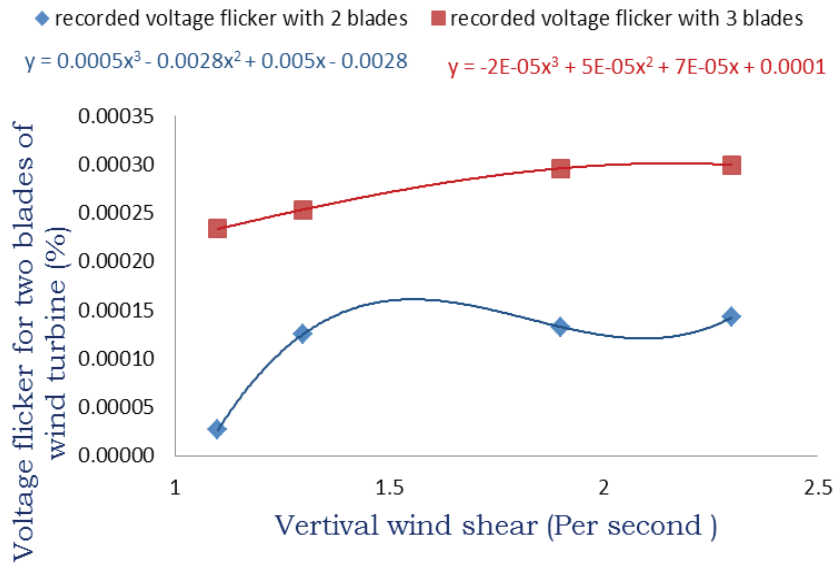


Figure 3: Comparison of flicker initiated by different number blades of wind turbine

In the fig. 3 impact of number of blades on flicker initiated in wind turbine is represented. For three blades the flicker produced is higher than two bladed wind turbines. In three bladed wind turbine because of 3p effect the flicker produced is more. As in three bladed wind turbine there is a three time jerk to the blades in one revolution. One jerk for each blade, in one revolution is produced when, the blade coincides with the tower.

Table 2  
Equations For Sixth Order Flicker Model For Different Number Of Blades

Number of blades	Equations by curve fitting for different wind turbine blades
2	$y = -0.0002x^4 + 0.0021x^3 - 0.0067x^2 + 0.009x - 0.0043$
3	$y = -4E-05x^4 + 0.0003x^3 - 0.0008x^2 + 0.0009x - 8E-05$

Table 3  
Constant in sixth order flicker model for different number of blades

Constants	Order of Vshr	Number of blades of wind turbine	
		2	3
A	6	0	0
B	5	0	0
C	4	-0.0002	-4E-05
D	3	+ 0.0021	+ 0.0003
E	2	- 0.0067	- 0.0008
F	1	+ 0.009	+ 0.0009
G	0	- 0.0043	- 8E-05

## 7. PROPOSED SIXTH ORDER MODELS FOR DIFFERENT BLADE MATERIAL

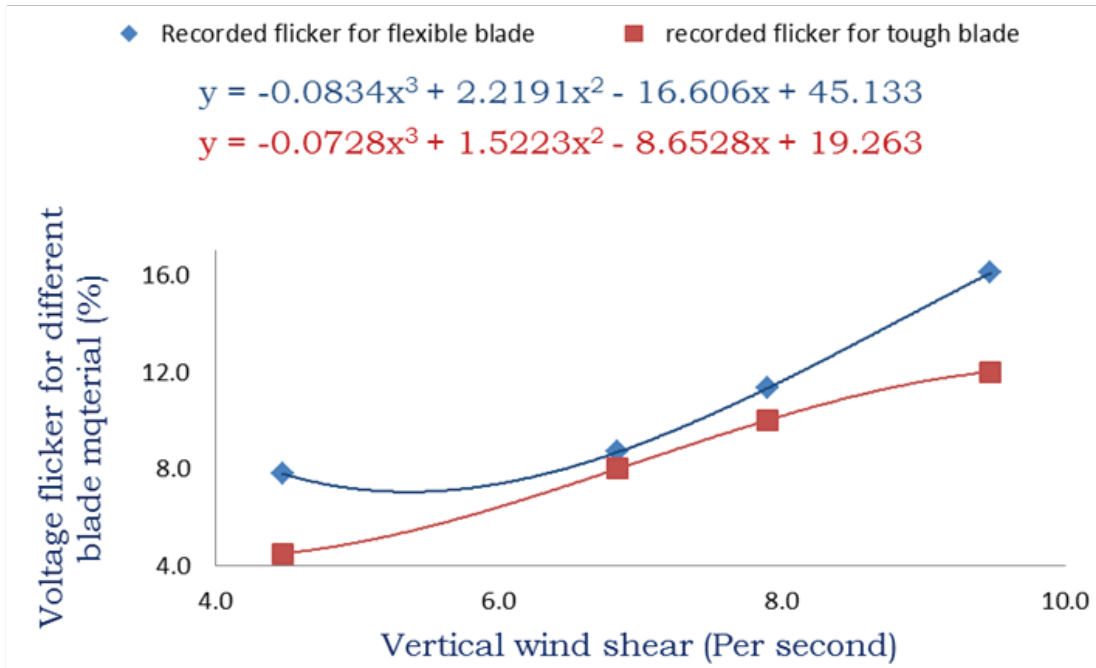


Figure 4 : Comparison of flicker initiated by different blade materials

**Table 4**  
Equations for sixth order flicker model for different blade materials

Blade material	Equations by curve fitting for different blade materials
Flexible	$y = -0.0834x^3 + 2.2191x^2 - 16.606x + 45.133$
Tough	$y = -0.0728x^3 + 1.5223x^2 - 8.6528x + 19.263$

**Table 5**  
Constant in sixth order flicker model for different blade materials

Constants	Order of vsshr	Blade material of wind turbine model	
		Flexible	Tough
A	6	0	0
B	5	0	0
C	4	0	0
D	3	-0.0834	-0.0728
E	2	2.2191	1.5223
F	1	-16.606	-8.6528
G	0	45.133	19.263

## 8. PROPOSED SIXTH ORDER MODELS FOR DIFFERENT BLADE LENGTHS

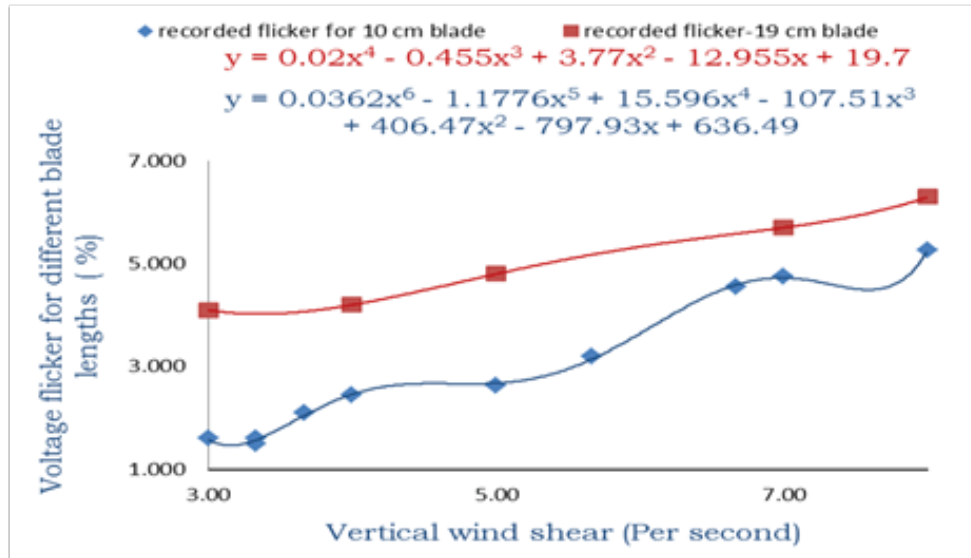


Figure 5: Comparison of flicker initiated by different blade length

Table 6  
Equations For Sixth Order Flicker Model For Different Blade Length

Blade length	Equations by curve fitting for different blade lengths
10	$y = 0.0362x^6 - 1.1776x^5 + 15.596x^4 - 107.51x^3 + 406.47x^2 - 797.93x + 636.49$
19	$y = 0.02x^4 - 0.455x^3 + 3.77x^2 - 12.955x + 19.7$

Table 7  
Constant In Sixth Order Flicker Model For Different Blade Lengths

Constants	Order of Vshr	Blade length of wind turbine model	
		10 cm	19 cm
A	6	0.0362	0
B	5	- 1.1776	0
C	4	+ 15.596	0.02
D	3	- 107.51	- 0.455
E	2	+ 406.47	3.77
F	1	- 797.93	- 12.955
G	0	+ 636.49	+ 19.7

## 9. PROPOSED SIXTH ORDER MODELS FOR DIFFERENT BLADE WIDTH

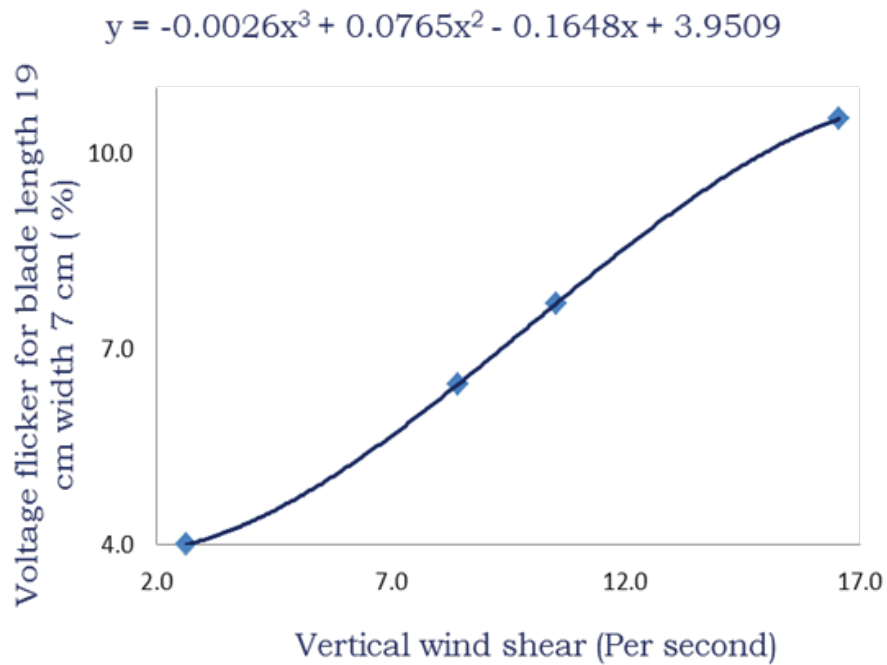


Figure 6: Vertical wind shear for blade length 19 cm width 7 cm

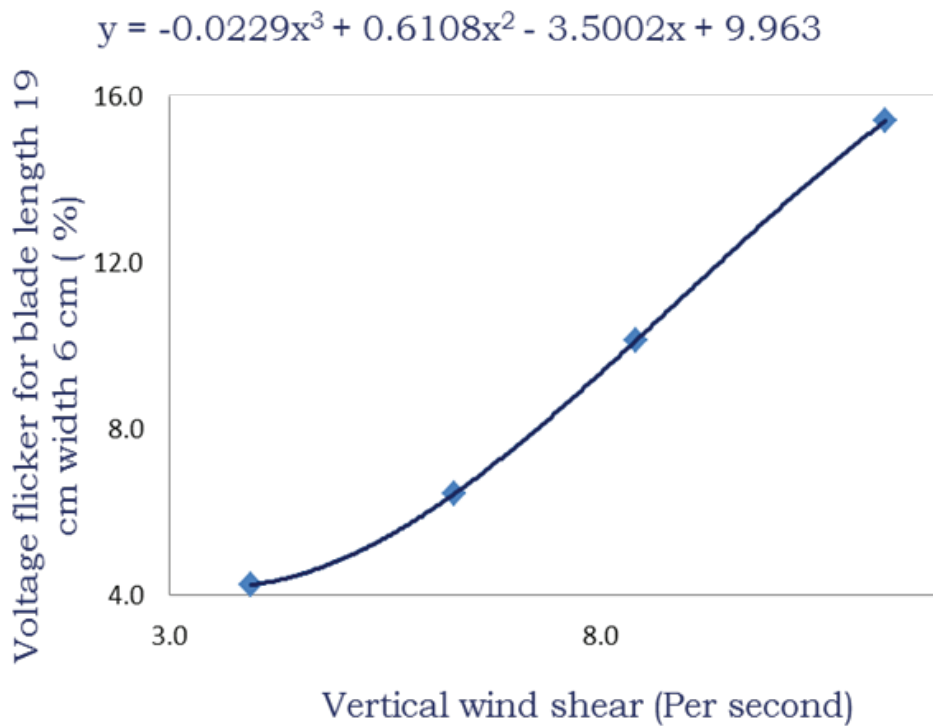


Figure 7: Vertical wind shear for blade length 19 cm width 6 cm



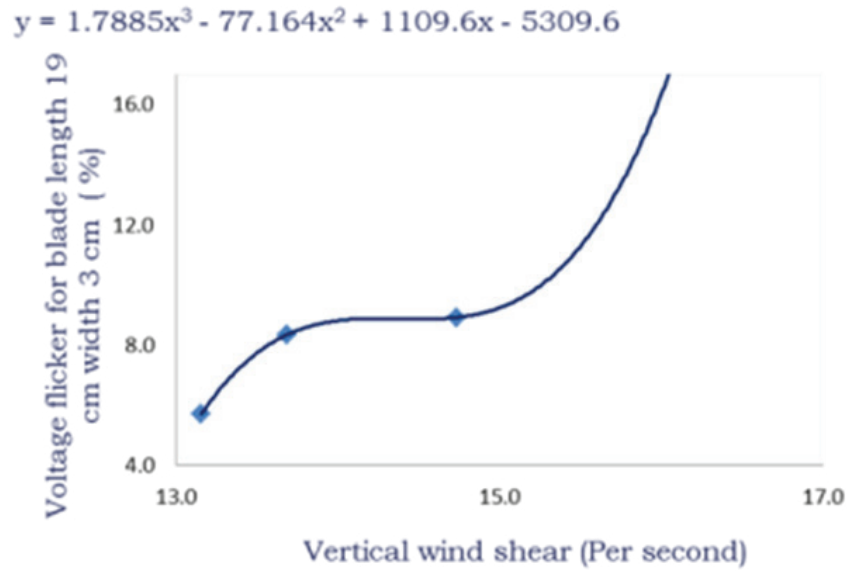


Figure 8: Vertical wind shear for blade length 19 cm width 3 cm

Table 8  
Sixth Order Equations For Different Chord Lengths I.e. Width Of Blades

Blade width (cm)	Equations for different blade width. Blade length 19 cm
7	$y = -0.0026x^3 + 0.0765x^2 - 0.1648x + 3.9509$
6	$y = -0.0229x^3 + 0.6108x^2 - 3.5002x + 9.963$
3	$y = 1.7885x^3 - 77.164x^2 + 1109.6x - 5309.6$

Table 9  
Constant in Sixth Order Flicker Model For Different Chord Lengths i.e. Width of Blades

Constants	Order of vs <sub>hr</sub>	Fixed blade length 19 cm, Blade width as given below		
		7 cm	6 cm	3 cm
A	6	0	0	0
B	5	0	0	0
C	4	0	0	0
D	3	- 0.0026	0.0229	1.7885
E	2	+ 0.0765	+ 0.6108	- 77.164
F	1	- 0.1648	- 3.5002	+ 1109.6
G	0	+ 3.9509	+ 9.963	- 5309.6

**Table 10**  
**Comparison Of Constants Of Sixth Order Equations For Various Parameters of Wind Energy**

	Constants	A	B	C	D	E	F	G
Parameters								
Blade length	10 cm	0.03	- 1.17	15.59	- 107	406.4	- 797	636.4
	19 cm	0	0	0.02	- 0.45	3.77	- 12.9	19.7
Blade width	7 cm	0	0	0	- 0.00	0.07	- 0.16	3.95
	6 cm	0	0	0	0.02	0.61	- 3.50	9.963
	3 cm	0	0	0	1.78	- 77.1	1109	- 5309
Number of blades	2	0	0	-0.0	+ 0.00	- 0.00	0.0	- 0.00
Number of blades	3	0	0	-0.00	+ 0.0	- 0.00	0.0	- 0.00
Type Of Blade	Flexible	0	0	0	- 0.0	2.21	- 16	45.1
	tough	0	0	0	- 0.0	1.52	- 8.65	19.2

## 10. BOUNDARY CONDITIONS OF THE PROPOSED EMPIRICAL MODELS

In this section various boundary conditions of the voltage flicker models developed are given. These developed models are for horizontal axis upwind turbine.

1. Useful for horizontal axis wind turbine, as vertical axis wind turbine is installed at a ground level and there is no question of tower height.
2. Suitable for three bladed turbines. Experiment is carried out on three bladed wind turbines as most of the turbines have three blades. Two blade turbines are rarely used.
3. Suitable for fixed speed wind turbine. In variable speed wind turbine normally doubly fed induction generator along with convertor is incorporated. Most of the power quality issues are dealt over there but harmonics are initiated in the system because of electronic power devices.
4. Suitable for large wind turbines with longer blades. For smaller blades the wind speed on each blade is almost equal and wind shear effect is less.

In this section various boundary conditions of voltage flicker models are given.

Sixth order model is the best suited model. Assumptions during development of model and boundary conditions of developed voltage flicker model.

**Table 11**  
**Sixth Order Model of Voltage Flicker**

Type of Voltage flicker Model	Constant	Mathematical model
Curve fitting	With constant	$P_{st} = 0.0544 V_{shr}^6 - 1.7039 V_{shr}^5 + 21.835 V_{shr}^4 - 146.18 V_{shr}^3 + 538.61 V_{shr}^2 - 1034 V_{shr} + 809.02$

In the fig. 9 graphs of voltage flicker verses vertical wind shear for various order models are given. The curve fitting sixth order model is shown by dotted lines. Curve fitting model is the best fitted model.

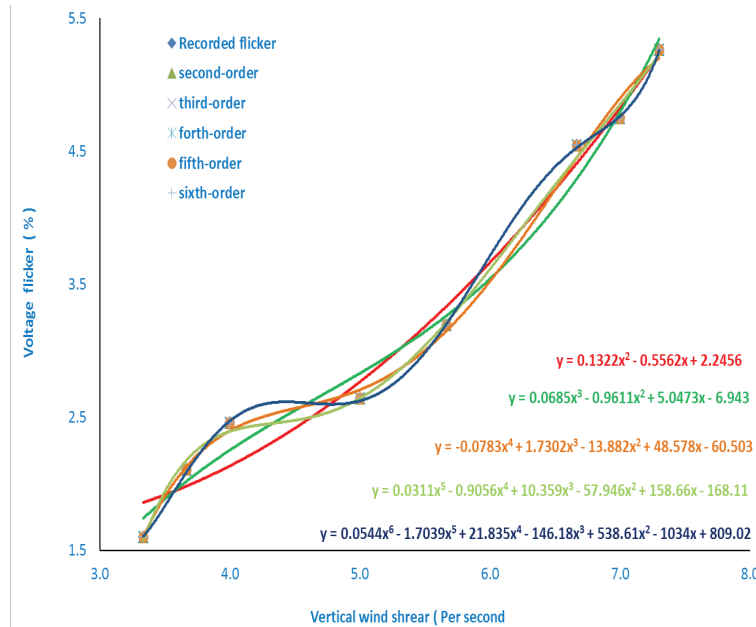


Figure 9: Comparison of various order graphs with sixth order graph

The graph of second order, third, fourth order, fifth order and sixth order are given. The sixth order model is the best fitted model. The models are obtained by curve fitting technique. The equations of the graphs re also obtained.

From the recorded RMS voltage, average voltage is computed. The change in the voltage is computed as well. The ratio of change in the voltage to the average voltage is multiplied by hundred to get percentage voltage flicker.

Table 12 shows sample calculation for computation of vertical wind shear from recorded values of wind speed at the top and bottom sided blade of the wind turbine.

Table 2  
Computation Of Vertical Wind Shear

Speed at top sided blade of wind turbine (m/s)	Speed at bottom sided blade of wind turbine (m/s)	Average wind speed (m/s) Refer equation 4.1	Change in the wind speed Refer equation 4.2	Vertical wind shear (per second) Refer equation 4.3
6.8	5.9	6.35	0.9	3.0
5.4	4.4	4.9	1.0	3.3
6.6	5.6	6.1	1.0	3.3
5.3	4.2	4.75	1.1	3.7

## 11. CONCLUSIONS

In this paper various models are developed. Second order, third order, forth order, fifth order and sixth order model of flicker are developed. Out of these models sixth order models is the best suited model for computation of flicker.

## 12. ACKNOWLEDGMENT

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## REFERENCES

- [1] J. J. Gutierrez; J. Ruiz; L. A. Leturiondo; A. Lazkano ,“ Flicker Measurement System for Wind Turbine Certification”, IEEE Transactions on Instrumentation and Measurement 2008, Vol. 57, Issue: 12, pp. 375 – 382.
- [2] Larsson, A.,“Flicker emission of wind turbines during continuousoperation”, *IEEE Trans. Energy Conversion*,vol.17 , Issue: 1 2002, pp. 114 – 118.
- [3] Tao Sun ;Zhe Chen ;Blaabjerg, F. ,“Flicker study on variable speed wind turbines with doubly fed induction generators ”,*IEEE Trans. Energy Conversion*,vol. 20 , Issue 4, 2005 , pp. 896 – 905.
- [4] Vilar, C. ; Amaris, H. ; Usaola, J.,“Propagation of Flicker in Electric Power Networks Due to Wind Energy Conversions Systems”,*IEEETrans.Power Engineering*, vol. 22, Issue 5, 2002 ,pp. 65 – 66.
- [5] Barahona, B.; Sørensen, P.; Christensen, L.; Sørensen, T.; Nielsen, H.K.; Larsén, X.G. ,“Validation of the Standard Method for Assessing Flicker From Wind Turbines”,*IEEE Trans. Energy Conversion* vol. 26 , Issue 1, 2011 , pp. 373 – 378.
- [6] Heier, Siegfried (2005). Grid Integration of Wind Energy Conversion Systems. Chichester: John Wiley & Sons. p. 45. ISBN 0-470-86899-6.
- [7] Harrison, Robert (2001). Large Wind Turbines. Chichester: John Wiley & Sons. p. 30. ISBN 0-471-49456-9.
- [8] Lubosny, Zbigniew (2003). Wind Turbine Operation in Electric Power Systems: Advanced Modeling. Berlin: Springer. p. 17. ISBN 3-540-40340-X.
- [9] Gregory M. Gallina (2002)Environmental Vertical Wind Shear and Tropical Cyclone Intensity Change Utilizing Enhanced Satellite Derived Wind Information University of Wisconsin--Madison, 2002 - 266 pages
- [10] Roger C. Dugan, Mark F. Mcgranaghan, Surya Santosa and H. Wayne Beaty, book on Electrical Power System Quality, Tata McGrahill. 2008, pp. 28-37.
- [11] Richard L. Hills, “power from wind”, Cambridge University Press, Great Britain. Papers from Conference Proceedings (Published):
- [12] M. E. Weber; M. A. Isaminger; C. Meuse; S. V. Vasiloff; T. Shepherd ,“ Comparative analysis of ground-based wind shear detection radars”,*Proceedings International Radar Conf.*,1995, pp. 486 – 495.
- [13] Datta. S. Chavan; Pooja Kulhari; Nehal Kadaganchi; P. B. Karandikar; Puneet Singh; Rajesh Giri,“Prediction of power yield from wind turbines for hilly sites”, IEEE 2nd International Future Energy Electronics Conf. (IFEEEC), 2015, pp. 1 – 5.
- [14] Datta. S. Chavan; P. B. Karandikar ,“ Assessment of Flicker Due to Vertical Wind Shear in a Wind Turbine Mounted on a Hill with Linear Approach”, 4th International Conference on Artificial Intelligence with Applications in Engineering and Technology, 2014, pp. 259 – 263.
- [15] Xue zhu Lv; Xiaofeng Li; Xiaofeng Yang; William Pichel; Xuan Zhou; Yuguang Liu ,“ The impact of vertical wind shear on the hurricane eye tilt at the sea and cloud levels”, 2013 IEEE International Geoscience and Remote Sensing Symposium - IGARSS, 2013, pp. 566 – 569.
- [16] Datta. S. Chavan; P. B. Karandikar ,“ Linear Model of Flicker Due to Vertical Wind Shear for a Turbine Mounted on a Green Building”, 4th International Conference on Artificial Intelligence with Applications in Engineering and Technology, 2014, pp. 253 - 258.
- [17] Datta. S. Chavan; P. B. Karandikar; Abhay Kumar Pande; Santhosh Kumar ,“ Assessment of flicker owing to turbulence in a wind turbine placed on a hill using wind tunnel”, International Conference on Circuits, Power and Computing Technologies [ICCPCT-2014], 2014, pp. 560 – 566.
- [18] Q. Jin; M. Wu; Z. G. Fan; W. Ding,“ Availability evaluation of wind farms considering the influence of vertical wind shear”, Fifth Asia International Symposium on Mechatronics (AISM 2015), 2015, pp.: 1 – 5.

- [19] Datta. S. Chavan; P. B. Karandikar; Abhay Kumar Pande; Santhosh Kumar ,“Computation of flicker as a result of turbulence in a wind turbine sited on a green building using wind tunnel”, International Conf. on Circuits, Power and Computing Technologies [ICCPCT-2014], 2014, pp. 554 – 559.
- [20] Datta. S. Chavan; Aditi Rana; Mahal Raj Singh; P. B. Karandikar; S. D. Bhide ,“ Empirical model of flicker due to vertical wind shear instigated by civilization in a seashore wind turbine using wind tunnel”, 2nd International Conf. on Devices, Circuits and Systems (ICDCS), 2014, pp. 1 - 7.
- [21] K. Redondo; A. Lazkano; P. Saiz; J. J. Gutierrez; L. A. Leturiondo; I. Azkarate ,“ Effects of digital differentiation on flicker measurements in wind turbines”, 2014 16th International Conf. on Harmonics and Quality of Power (ICHQP) 2014, pp. 263 – 267.
- [22] Datta. S. Chavan; Aditi Rana; Mahal Raj Singh; P. B. Karandikar; S. D. Bhide ,“ Modeling of flicker due to vertical wind shear initiated by vegetation in a riverside wind turbine using wind tunnel”, 2nd International Conference on Devices, Circuits and Systems (ICDCS), 2014, pp. 1 – 6.
- [23] Datta. S. Chavan; Aditi Rana; Mahal Raj Singh; S. S. Deo; P. B. Karandikar ,“ Computation of flicker due to vertical wind shear in a wind turbine sited on a hill using wind tunnel”, IEEE 8th International Power Engineering and Optimization Conference (PEOCO2014), 2014, pp. 231 – 236.
- [24] Ali H. Kasem Alaboudy; H. H. Zeineldin ,“ Flicker minimization of DFIG based wind turbines with optimal reactive current management”, 2011 IEEE PES Conference on Innovative Smart Grid Technologies - Middle East, 2011, pp. 1 – 5.
- [25] Datta. S. Chavan; Aditi Rana; Mahal Raj Singh; S. S. Deo; P. B. Karandikar ,“ Modeling of flicker in wind turbine on a green building due to vertical wind shear”, IEEE 8th International Power Engineering and Optimization Conf. (PEOCO2014), 2014, pp. 225 – 230.
- [26] Datta. S. Chavan; S. D. Bhide; P. B. Karandikar ,“ Effect of vertical wind shear on flicker in wind farm”, IEEE Global Humanitarian Technology Conf. South Asia Satellite (GHTC-SAS), 2013, pp. 203 – 208.
- [27] Y. A. Kazachkov , J. W. Feltes and R. Zavadil “Modeling wind farms for power system stability studies”, *Proc. IEEE Power Eng. Soc. Gen. Meeting*, pp.1526 -1533 2003
- [28] J. M. Rodriguez , J. L. Fernandez , D. Beato , R. Iturbe , J. Usaola , P. Ledesma and J. R. Wilhelmi “Incidence on power system dynamics of high penetration of fixed speed and doubly fed wind energy systems: Study of the Spanish case”, *IEEE Trans. Power Syst.*, vol. 17, no. 4, pp.1089 -1095 2002
- [29] N. R. Ullah , A. Larsson , A. Petersson and D. Karlsson “Detailed modeling for large scale wind power installations—A real project case study”, *Proc. 3rd Int. Conf. Elect. Utility Deregulat. Restruct. Power Technol.*, pp.46 -56 2008
- [30] J. B. Ekanayake , L. Holdsworth , W. XueGuang and N. Jenkins “Dynamic modeling of doubly fed induction generator wind turbines”, *IEEE Trans. Power Syst.*, vol. 18, no. 2, pp.803 -809 2003
- [31] V. Akhmatov , A. H. Nielsen , J. K. Pedersen and O. Nymann “Variable-speed wind turbines with multi-pole synchronous permanent magnet generators. Part I: Modelling in dynamic simulation tools”, *Wind Eng.*, vol. 27, no. 6, pp.531 -548 2003
- [32] T. Ackermann *Wind Power in Power Systems*, 2005 :Wiley
- [33] G. Ramtharan , N. Jenkins and O. Anaya-Lara “Modelling and control of synchronous generators for wide-range variable-speed wind turbines”, *Wind Energy*, vol. 10, no. 3, pp.231 -246 2007
- [34] L. Holdsworth , X. G. Wu , J. B. Ekanayake and N. Jenkins “Comparison of fixed speed and doubly-fed induction wind turbines during power system disturbances”, *Proc. Inst. Elect. Eng.—Gen., Transm. Distrib.*, vol. 150, no. 3, pp.343 -352 2003
- [35] P. Vas *Vector Control of AC Machines*, 1990 :Oxford Univ. Press
- [36] C. E. Ugalde-Loo and J. B. Ekanayake “State-space modelling of variable-speed wind turbines: A systematic approach”, *Proc. IEEE ICSET*, pp.1 -6 2010
- [37] P. C. Krause , O. Wasynczuk and S. D. Sudhoff *Analysis of Electric Machinery and Drive Systems*, 2002 :Wiley
- [38] M. O. L. Hansen *Aerodynamics of Wind Turbines*, 2008 :EarthscanPubl.